

Learning Module 10: Interest Rate Risk and Return

Fixed Income

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Duration Gap

$$\text{Duration gap} = \text{Macaulay duration} - \text{Investment horizon}$$

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### Duration Gap

$$
\text{\text{Duration gap}} = \text{\text{Macaulay duration}} - \text{\text{Investment horizon}}
$$
```

Macaulay Duration

The general calculation of Macaulay duration, $MacDur$, that also accounts for partial coupon periods if the calculation is done between coupon dates is shown in Equation 2.

$$MacDur = \left\{ \begin{aligned} &(1 - t/T) \left[\frac{PMT}{(1+r)^{1-t/T}} \right] + (2 - t/T) \left[\frac{PMT}{PV^{Full}} \right] + \\ &\dots + (N - t/T) \left[\frac{PMT+FV}{(1+r)^{N-t/T}} \right] \end{aligned} \right\} \quad (2)$$

Where:

- t is the number of days from the last coupon payment to the settlement date
- T is the number of days in the coupon period
- t/T is the fraction of the coupon period that has passed since the last payment
- PMT is the coupon payment per period
- FV is the future value paid at maturity, or the par value of the bond
- r is the yield-to-maturity per period; and
- N is the number of evenly spaced periods to maturity as of the beginning of the current period

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Macaulay Duration

The general calculation of Macaulay duration, $MacDur$, that also accounts for partial coupon periods

\$\$

MacDur =

\left\{

\begin{aligned}

(1 - t/T)\left[\frac{PMT}{(1+r)^{1-t/T}}\right]PV^{Full}\right]

+

(2 - t/T)\left[\frac{PMT}{(1+r)^{2-t/T}}\right]PV^{Full}\right]

```

+ \\
\cdots +
(N - t/T)\left[\frac{\frac{PMT + FV}{(1+r)^{N-t/T}}}{PV^{\text{Full}}}\right]
\end{aligned}
\right\} \tag{2}
$$

```

Where:

- t is the number of days from the last coupon payment to the settlement date
- T is the number of days in the coupon period
- t/T is the fraction of the coupon period that has passed since the last payment
- PMT is the coupon payment per period
- FV is the future value paid at maturity, or the par value of the bond
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- N is the number of evenly spaced periods to maturity as of the beginning of the current period

Macaulay Duration: Closed-Form

$$MacDur = \left\{ \frac{1+r}{r} - \frac{1+r + [N \times (c-r)]}{c \times [(1+r)^N - 1] + r} \right\} - \frac{t}{T} \quad (3)$$

Where:

- r is the yield-to-maturity per period
- N is the number of evenly spaced periods to maturity as of the beginning of the current period
- c is the coupon rate per period
- t is the number of days from the last coupon payment to the settlement date and
- T is the number of days in the coupon period

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Macaulay Duration: Closed-Form

$$\begin{aligned} & \$\$ \\ & \text{MacDur} = \\ & \left\{ \frac{1+r}{r} - \frac{1+r + [N \times (c - r)]}{c \times \left[(1+r)^N - 1 \right] + r} \right\} \\ & \frac{t}{T} \tag{3} \\ & \$\$ \end{aligned}$$

Where:

- r is the yield-to-maturity per period
 - N is the number of evenly spaced periods to maturity as of the beginning of the current period
 - c is the coupon rate per period
 - t is the number of days from the last coupon payment to the settlement date and
 - T is the number of days in the coupon period
-